MEMO #28

TO: W. BRUCKMAN DATE: AUGUST 22, 1990

FROM: P. CHEIMETS

SUBJECT: MEASUREMENT OF WIND AT MAUNA KEA SITE

cc: G. NYSTROM

R. DIAS L. COYLE

SCOPE:

The lack of good applicable wind spectrum data leads us to conclude that a set of measurements must be made at the proposed Mauna Kea site to use in predicting the antenna pointing and tracking performance. We wish to associate these measurements with an existing body of measured climate information for the area. This requires that spectrum measurements at the proposed site be coordinated with average weather condition measurements at one of the easterly summits.

Two sources of general wind information were reviewed, one from a Mauna Kea site survey performed for the University of Hawaii and the other from the the USAF Climatic Center at Hilo. These show a year round prevailing easterly flow, though the pattern is less pronounced in the winter. The site survey presents wind data taken on the three peaks that surround the proposed SMA site. The data seems to show that the two upwind (easterly) peaks disrupt the wind pattern measured at the downwind peak, and presumably in the valley between. Unfortunately the data was taken on the three peaks at different times, and therefore are inconclusive.

A proposed wind experiment is described, complete with the data logging hardware.

INTRODUCTION:

We are developing a SMA antenna pointing and tracking model to assist in the preparation of an overall system specification. Key to a successful model is an understanding of the influences and disturbances that the antenna is subject to. In this case the single largest external, non-systematic pointing disturbance is the wind. As mentioned elsewhere the wind causes problems in two frequency domains, first continuous flows cause a tracking offset, and second, wind variations with a frequency component near the position servo bandwidth will cause oscillations.

We have attempted to find useful wind speed data from the literature, and though this has yielded useful information on the average wind speed at the Mauna Kea site, all attempts to acquire accurate spectrum information have failed. Furthermore, there is not enough general information about mountain top climates to make a meaningful estimate extrapolating from measurements elsewhere. Using the general formulae for wind spectrum with rough values for the free parameters can result in a spectrum that is as much as 10

times different than the true spectrum. Therefore, a test to measure the wind spectrum at the proposed has been proposed.

The wind literature that we reviewed all conclude that a minimal amount of data is required to characterize the wind speed spectrum at a given location. A single spectrum determined from 100-500 seconds of rapidly sampled wind velocity data is enough to determine the general spectrum for a particular wind direction at that site. For sites that have no unsymmetrical features this single measurement will tell you all you need to know about the wind in all directions.

The proposed SMA site is surrounded by several wind-effecting features that can, and the available data suggest, do influence the wind average speed and spectrum. There are two peaks to the east and a single summit to the west. These peaks are 100-200m higher than the plane that the antennas are to sit on and only 500-750m away.

In performing a wind spectrum measurement we would like to determine two things:

- What is the worst wind spectrum we are likely to encounter within the precise and degraded operating range (wind speed <15 m/s),
- 2) What is the wind speed spectrum of the prevailing, or most likely wind.

These questions are separate because the site presents different features to the wind when approached from different directions. The first question can be answered by measuring wind spectra for winds in all directions. The second question is a little more difficult since the wind pattern at the site has not been measured enough to determine what the prevailing patterns are. We can make the assumption though, that the wind at the site during a period of prevailing wind at the summit is the prevailing wind. This suggests a simultaneous measurement of average wind speed at one of the eastern summits while the spectrum measurements are being made.

We spoke with the Hawaiian Bureau of Land Development to get wind direction data on the Mauna Kea site that would tell us what the prevailing winds were and in what season they were most likely to occur. This would indicate the most favorable time to perform the survey. They sent us two compilations of wind data from the island of Hawaii. Both are appended to this memo and summarized below.

The first survey is a listing of wind measurements taken over Hilo airport at an altitude of 3050 m, during the 11 year period between 1950 and 1961. These indicate a prevailing easterly flow at an average speed of 5.3-6.8 m/s throughout the year. The wind speed is below 10 m/s 90 % of the time, except in the winter when it exceeds this value 20 % of the time. The flow is within 22 deg of east 50 % of the time in the summer and fall, dropping to 30 °

in the winter. In the winter and spring the wind is westerly 20 % of the time, it is hardly ever westerly in the summer and fall.

The second source of information on the mountain climate is a Mauna Kea site survey made over a year period between 1965-1966. This survey tracked winds on the three summits that immediately surround the proposed site. The data seem to show a tendency for the eastern summits to divert the flow, changing the apparent wind direction at the third summit, which is on the other side of the site; the implication being that the wind in the valley between is also affected. Unfortunately the data cannot be used to say anything that strongly since the periods during which the measurements were made on the three summits do not overlap. The measurements at the easterly summits were made during the months from April to December while the wind speed and direction were measured to the west between November and March, thus only overlapping a month, December and only measuring in the west during the least representative time during the year, winter. The fact that the western peak showed little easterly wind while the eastern peak showed a lot can be partially explained by the timing of the measurements.

It is still fair to say that the proposed site is not a general site with relationship to the wind, its direction or spectrum. There is still reason to believe that the plateau is in the wake of the two eastern summits and that they will cause a change in the apparent wind direction, average speed and spectrum. Furthermore an argument can be made that the apparent wind direction at the site will vary with wind speed at the summit without the apparent wind direction at the summit to a spectrum is also a function on the summit wind speed, since this implies that the site is falling in and out of the wind wake of the eastern summits.

A test program that is intended to determine the likely wind induced disturbances to the antennas must take all these possibilities into account as well as the location on the site where the antenna might be. We are therefore proposing to measure at various points in the site and at various summit wind conditions.

TEST OUTLINE:

The test is a simple one, sample the wind speed at a short sampling period for 100 or so seconds under a variety of summit conditions. In order to produce meaningful information about wind speed variation up to the system bandwidth (in this case 10 Hz) the sensor must be able to respond to variations in excess of that rate and the signal must be sampled at at least twice the bandwidth, about a frequency of 20 Hz.

This relatively high frequency rules out the use of most wind sensors. The standard 3-cup anemometer responds up to about .5 Hz, the standard hot wire responds to variations up to 2 Hz. This limited the search to very thin hot wire or film probes, or a pitot

tube mounted on a fast pressure transducer.

Most of the hot wires are mounted in directional mounts and have to be pointed into the wind just like a pitot tube. The hot films, though they do not have to be pointed up wind are very expensive, and like the wires, can be damaged by rain. It was decided therefore that the sensor would be a pitot tube connected to an inexpensive pressure transducer, a semiconductor type made by SENSYM, and costing \$75 including conditioning electronics. The pitot tube is mounted on a wind vane that points it up into the wind.

The data gathering strategy is simple, two local computers, synchronized with each other, constantly track the wind speed and direction. One is on one of the summits at Mauna Kea the other is somewhere on the proposed site. When a certain condition is observed for the first time by the computer at the site, e.g. $_5$ m/s wind from the southeast, the computer begins to log data from our weather station, taking data at 20 Hz for about 100 seconds (2000 data points). This condition is then removed from the list of trigger conditions and the system awaits another trigger condition. Between trigger conditions the computer at the summit and the data logging computer take weather data every minute or so. $\rm B_Y$ correlating the data gathered at the summit with that taken at the site we will be able to compare conditions at the proposed site to the years of weather data collected at the summit and above the island, and relate the measured spectrum to known prevailing conditions.

There is a potential problem with this approach, it assumes that there is a weather station at the summit that can be interfaced to the computer. This issue is unresolved at this time, we are looking into it. Since there is a prohibition against radio transmitters in the science preserve we have structured the data logging to be triggered by a condition at the site. This avoids the two computers having to communicate remotely. There is the possibility of some ambiguity resulting from this approach, but that will become apparent quickly.

TRANSDUC ER PERFORMANCE

The pressure transducer must posses two attributes, high resolution to track the very small pressure fluctuation that result from wind speed variations, and rapid response. To determine that the selected transducer met these requirements several simple tests were run. First the high pressure port on the differential transducer was connected to an oil manometer. The manometer is a Dwyer product specifically designed for use with wind measuring pitot tubes. A syringe was inserted into the connecting tube and used to pressurize the inside to the desired levels, as determined from the manometer. The pressure transducer was calibrated and various intermediate pressures were placed on it. The absolute accuracy was found to be about .7 m/s with resolution and repeatability better than .5 m/s. There seems to be a slight nonlinearity through the calibration range, this can be removed by

look up tables.

The test of the transducer to a dynamic input was performed by connecting a tube to the high pressure port of the transducer, crimping the far end shut, and rapidly squeezing and releasing it. The squeezing action was performed by rotating an eccentric over the tube at various RPM. The output of the transducer was tracked with a storage scope. The output measured between 60 and 62 mV for crimping rates between 5 and 20 Hz. This correspond to a pressure change of around 2522 Pa, determined from calibration. This compares to an expected pressure variation of 2580 Pa, virtually identical.

WIND VANE:

The wind speed is measured by comparing the dynamic to the static pressure. This is done by putting one pressure tap directly into the wind while having another one always perpendicular to the wind (see Figure). In the present experiment the proposed method is to use a simple weather vane to point the dynamic tap or pitot tube into the wind and a downward pointing tap to register static pressure. The taps will each be connected to one of the ports of a differential pressure transducer.

The vane consists of a pitot tube and split tail mounted on a pivot, the wind forcing it to point upwind. The dynamic pressure is carried from the moving vane to a stationary tube through a lightly loaded oring in the pivot bearing. The tail is split to increase the restoring torque caused by a given wind. An internal cavity in the slip joint can be filled with a high viscosity fluid to increase damping, if this becomes necessary.

DATA LOGGER:

Presently we propose to use one of a variety of very low power computers designed specifically for the purpose of recording data in the field. The computers require very little power and can run for weeks without intervention, given that the amount of data that is being taken does not exceed the on board storage capacity. In our case the total data storage requirement is easy to calculate. Static ram boards are added until the memory requirements are met.

The computer will be enclosed in a weather tight container, probably made from a modified standard equipment case. If we determine that the power requirements are greater than the battery pack we may include a solar panel to recharge the batteries.

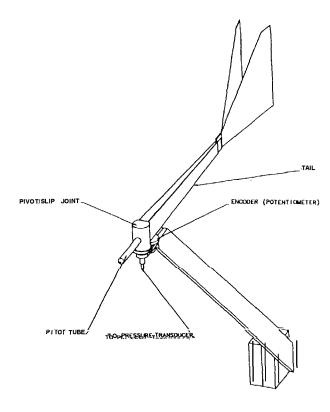


FIGURE SCHEMATIC OF WEATHER VANE

DATA REDUCTION:

Data reduction can be handled in a number of ways. The most likely approach is to perform a Fourier transform on the data and smooth it to remove spikes and drop outs. Then we can compare it to 50 years worth of accumulate wind spectrum data to determine the relevant modelling parameters, this will help ensure that we have good, consistent data. More simply we can use the measured data, as is, as an input to a control model of the antenna. This will give us an estimate of pointing performance immediately. Different pointing control methods can be examined to determine those that have the most likelihood of achieving the desired specification.

ישנווטי, יטוווטי Data sing Division 2150th Neather Squadron) PERCENTAGE (

WINDS ALOFT SYMMARY

BY SPEED GROUPS

21504 HILD, HAWAII TH WEAP

RINTER

RAHINS

MUSH 10,5 - 3,4

STATION

MO OR SEASON

TYPE OF OBSERVATION

50 51 52 53 54 55 56 47 58 59 60 61

					YEARS										
SPEED	M/S 1-4	5-10	11-15	16-20	21-25	26.30	31-38	39-51	52-77	78-102	≥ 103	TOTAL A	LL OBS	SPEED (KNO	TS)
	KNOTS 1-9	10-19	20.29	30-39	40-49	50-59	60.74	75-99	100-149	150-199	≥ 200			SI EED (KM	
DIR	M.P.H. 1-1		23-33	34-45	46-56	57 68	69-85	86-114	115-172	173-229	≥ 230	085.	%	รบพ	MEAN
N	52		Ó	1 T								116	5.3	1243	10.
NNE	44			I								114	5.2	1333	11.
NE	36	1	20	6	1							147	0.7	2137	14.
ENE	51			10								196	8.9	2832	14.
E	5:	164	55	13	7				1			289	13.1	4581	15.
ESE	41	118	26	2						i		194	8.8	2712	14.1
SE	3,	68		1	†———				ļ	1		116	5.3	1375	11.
SSE	3	61	7	3								108	4.9	1207	11.
5	4.	2 56	15	5	1							119	5.4	1537	12.
SSW	29	52	17	5								103	4.7	1428	13.
s w	4(71	19	8	5	1			†	 		151	6.8	2327	15.
WSW	3	74	25	12	1			i	<u> </u>			149	6.8	2319	15.0
w	4	77	27	10	ı					1		164	7.4	2413	14.
WNW	30	35	7	2								74	3.4	832	11.
N W	31	48	5	2		-						93	4.2	1006	10.1
N N W	21	28	3	1								ठ०	2.7	695	10.
CALM		- 										12	-5		
		 	-						 						
TOTALS	461	1147	283	82	11	1	1					2205	·-	46.006	13.6
ERCENT	30.5	52.0	12.8	3.7	.5	.0	٥.					1	100.0		
\$100	г -	7 19 0	24.4		43.4		70.0			1		,			
(Yerroup	5.7		24.4	34.0			70.0		<u> </u>	(5)					
		٧,	(y .	Σ	XY		ΣV ²	*	Nσ _y /Σχ	**a _v /V	σ_{c}	. .	σ _b ,	,

112	2.2744	15.660	Σχγ 50138.049	Σν ² 551876.313	* Nσ _γ /Σχ ' 4.464	**°,/\	12.816 8.9	99 9.048
N 2205	ΣX/N 2.113	12.500	SUM OF E COMPONENTS(ΣX) 4659.445	Σχ ² 354239.503		**°,/°.	.208 1.4	24
¥ 1 a	ΣΥ/N _ 44 1		SUM OF N COMPONENTS(ΣΥ) 1854.739-		* No _y /ΣΥ 11.213-	· **∀,/⊽ • • 17	Σγ 30036 13.6	

 $[\]sigma_{\rm c}$ Standard devotion of east components

AWS HQ FORM 0-46

V Scalarwnd speed

 θ Resultant wind direction V. Resultant wind speed

o. Standard deviation of wind components along the major axis of the distribution

 $\sigma_{\rm L}$ Standard deviation of wind components perpendicular to the major $\sigma_{\rm X|A}$ of the distribution

 ψ Angle of rotation of the major axis of the wind distribution counter-clockwise from E-W direction

PREVIOUS EDITIONS OF THIS FORM ARE OBSOLETE.

MATS 60 66

 $[\]sigma_{_{\mathrm{V}}}$ Standard deviation of north components

o Standard vector deviation of wind velocity

Correlation coefficient of north and east components

Average wind speed

[.] Ratio of standard deviations= σ_a/σ_b

 $[\]sigma_{\star}$ Standard deviator of wind speeds

Wherever ratio ~1000.0000, printed 999.9999

^{**} Wherever ratio ≥100.00, printed 99.99

Climat' Center, USAh Date Sing Division 2150th Weather Squadron

PERCENTAGE OF DIF NS

WINDS ALOFT ""MARY

BY SPEED GROUPS

21504 HILO, HAWAII IH WBAP SPRING

HAWINS
TYPE OF OBSERVATION

700 Mb

LEVEL

station station name Mo.orseason so, 51 52 53 54 55 56 57 58 5Y 60 61

91

YEARS

						TEARS										
SPEED	JK/8 1		10	11-15	16-20	21-25	26.30	31-38	39-51	52-77	76-102	≥ 103	TOTAL A	LLOBS	SPEED (KN)TG)
	KNOTS 1.		-19	20-29	30-39	40-49	50 59	60-74	75-99	100-149	150-199	≥ 200	. = 1712 7		TIEED (KM)	
DIR	M.P.H. 1-		- 2 2	23-33	34-45	46-56	57-68	69-85	86-114	115-172	173-229	≥ 230	OBS.	%	5 U M	MEAN
Ņ	4	- 1	4.2	4	!			1					76	4.1	894	9.
NNE	6	- 1	47	3									117	5.0	1010	8.6
NE	5		79	5	1								143	6.1	1496	10.5
ENE	7		151	29	5								264	11.3	3372	12.8
E	9		199	47	4	i.		İ	į				347	14.3	4641	13.4
ESE	7		108	13	Z								198	8.4	2304	11.6
SE	5		65	8	T					1			133	5.7	1476	10.7
SSE	4		37	2	1								83	3.5	808	9.7
5	3	-	44	5	1								67	3.7	923	10.6
5 5 W	4	- 1	40	5	3								88	3.8	971	11.0
5 W	4		65	29	8							·	146	6.2	2018	13.8
w sw	5		69	24	5								152	6.5	2051	13.5
w .	7		83	28	3	l							186	7.9	2370	12.7
WNW	3		47	6									112	4.8	1049	9.4
N W	6		30	3									99	4.2	816	8.2
N. N. W	4	5 j	38	2	ij				ĺ				86	3.7	802	9.3
CALM													Ð	• 3		
TOTALS	94	5 1	144	213	33	2							2345	-	26951	11.5
ERCENT	40.	3 4	6.8	9,1	1.4	<u>. 1</u>			! !				-	100.0		
MEAN SPEED (KNOTS)	5.	5 1	3.5	24.3	33.4	44.7										

•	٧,	۰ ×	}	Σγ²	* Na _v /2X	1 ** 0 . / Y .	σ,	. σ	σ
 99	2.0437	13.212	32070.444	418952.353	3.674	6.46	11.077	7.202	6.826
N	Σχ/Ν	σ _×	SUM OF E COMPONENTS(EX)	Σx ²	* Nσ _x /ΣX	** 0, /0,	r	* .	
2345	2.017	10.939	4729.474	290013.230	5.424	1.94	+177	1.538	
Ψ	ΣY/N	σ,	SUM OF N COMPONENTS(EY)	$\Sigma \gamma^2$	* Nσ _V /ΣΥ	** Y _r /_	Σγ	7 7	
12	. 330-	7.409	774.153-	128939.112	22.444-	-18	26951	11.5	

σ Standard devation of east components

σ, Standard deviation of northcomponents

σ_v Standard vector deviation of wind velocity

Correlation coefficient of north and east components

V Average wind speed

V Scaler wnd speed

⁴ Ratio of standard deviations=σ_α/σ_k

σ Standard deviation of wind components along the major axis of the distribution

 $[\]sigma_b$ Standard deviation of wind components perpendicular to the major axis of the distribution

Ψ Angle of rotation of the major axis of the wind distribution counter-clackwise from E-W direction

 $[\]theta$ Resultant wind direction

V_r Resultant wind speed

σ, Standard deviation of wind speeds

^{*} Wherever ratio ~1000.0000, printed 999.9999

^{**} Wherever ratio E100.00, printed 99.99

(FREQUENCY) OF DIPTIONS BY SPEED GROUP.

21504 HILO. HAWALL TH WHAP

SUMMER

RAWINS

700

MO. OR SEASON

TYPE OF OBSERVATION

LEVEL

50 **51 52 53 54 95 56 97** 50 59 60 61

						YEARS										
SPEED	M/S -	_	5.10	11-15	16-20	21-25	26-30	31-38	39-51	52:77	78.102	≥ 103	TOTAL A	LL OBS	SPEED (KN	OTS)
	KNOTS I-	_	10-IS	20-29	30.39	40-49	50-59	60-74	75-99	100-149	150-199	≥ 200				
DIR	M.P.H. I-		11-22	23.33	34-45	46-56	57-68	69-85	86-114	115-172	173 229	≥ 230	OBS.	%	SUM	MEAN
N	4		47						-		<u> </u>		93	4.0	सम्प	9.1
NNE	Ü	- 1	45	1 0									113	5.2	1105	9.
NE	8		106	10			~~				<u> </u>		201	8.7	2129	10.8
ENE	10		204	33					I		1		345	15.0	4370	12.
E	13		363	77	F	'							583	25.4	7834	13.4
ESE	8		194	25							<u> </u>		303	13.2	3722	12.
SE	7		113	10		<u> </u>	<u> </u>		l		<u> </u>		[44	8.4	2154	11.1
SSE	4		47	4									97	4.2	989	10.2
S	4		34	2]								85	3.7	742	8.7
5 5 W	2		24	1									52	2.3	497	9.6
s w	2		12										34	1.5	264	7.8
WSW	2		10										34	1.5	225	6.6
W	2		12										41	L.R	252	6.9
WNW	2		9			<u> </u>					1		36	3.1	266	7.4
N W	2		6	1									2.9	1.3	212	7.3
NNW	2	8	19	1									45	2.0	. 369	8.2
CALM													8	• 3		
TOTALS	86	0	1242	173	14	L	r.1*		1				2799	-	26030	11.3
PERCENT	37.	4	54.0	7.5	. 6	.0			.0				-	100.0		
MEAN SPEED (KNOTS) IY GROUP	5.	6	13.3	23.5	33.9				07.0							
	89		7.724	2 10	7. 0.419	70	xy 963.768		Σγ² 386621		Nσ _y /Σχ		§5 8.	oii		324
	N 2299		ΣX/N 7.723		, 1.992	SUM OF E CO	mponents(∑ 755. <i>135</i>	-	Σχ ⁷ 283913		™nσ _x /ΣX 1.035	***0,/0		045	1.203	

- σ Standard devation of east components
- σ Standard deviation of north components
- a.. Standard vector deviation of wind velocity
- r Correlation coefficient of northand . 94

ΣΥ/Ν

. 136

- ▼ Average wind speed
- V Scalar wnd speed
- . Ratio of standard deviations= σ_a/σ_b

Standard deviation of wind components along the major axis of the distribution Standard deviation of wind components perpendicular to the major axis of the distribution

49.179

- Angle of rotation of the major axis of the wind distribution counter-clockwie from E-W direction

26030

.68

- Resultant wind direction
- Resultant wind speed
- Standard deviation of wind speeds
- Wherever ratio ~1000.0000, printed 999.9999

102708-178

** Wherever ratio \$100.00, printed 99.99

MATS 60.66

6.684

SUM OF N COMPONENTS(EY) 312.461

2 1 5 0 4 HILO, HAWAII TH WBAP 50°T451N 32 53 54 55 56 STATION NAME 57 58 59 60

AUTUMN MO. OR SEASON

RAHINS

MIL 100

TYPE OF OBSERVATION

LEVEL.

YEARS

					YEARS										
SPEED	M/S 1-4	5-10	11-15	16-20	21-25	26.30	31-38	39-51	52-77	78.102	≥ 103	TUIÁL A	LLORS	SPEED (KN	OTE)
\ \	KNOTS 1-9	10-19	20-29	30-39	40.49	50.59	60-74	75-99	100-149	150-199	≥ 200			JI LED (KIN	J13)
	M.P.H. 1-10	11-22	23.33	34-45	46.56	57-68	69-85	86-114	115-172	173-229	≥ 230	OBS.	%	SUM	MEAN
N	68	45				1						114	4.8	981	0.0
NNE	69	54	4									127	5.3	1142	9.0
NE	89	116										213	9.0	2205	10.4
ENE	91	236	50	3								380	16.0	5016	13.2
E	136	259	47									449	18.9	5730	12.8
ESE	77	118	16	1								212	8.9	2364	11.2
SE	75	67	2		l	.4l		<u> </u>			. "	144	.6.1	1317	9.1
SSE	दव	40	1									90	3.8	793	8.8
s	46	53	5									104	4.4	1072	10.3
S W	4a	34	4	2								82	3.5	822	10.0
wsw	33			2		1						93	3.9	956	10.3
		43	1									77	3.2	769	10.0
W	56		8									111	4.7	1127	10.2
\N N ₩	32	13				1						. 45	1.9	334	7.4
N W	3.5	7.9	2									58	2.4	455	7.8
IN N W	40	22				4 [62	2.6	456	7.4
CALM						<u> </u>						15	-6		
TOTALS	985	1204	156	14] t						2376	-	25539	10.7
ERCENT	41.5	50.7	6.6	.6		0							100.0		
BY GROUP	5.5	13.2	23.7	34.4		54.0									
	•	٧,		, l	· i	XY		ΣV ²	*	Νσ _γ /ΣΧ	**o _v /V	σ	<u>. </u>	σ _b	σ,

	•	٧,	a,	EXY	Σν2	* Nσ _V /ΣX	** 0 / V ,	σ	σ _b	σ.
	85	5.1301	11.247	34549.465	362980.597	1.330	2.19	9.182	6.496	6.104
ľ	И	ΣX/N	σ _x	SUM OF E COMPONENTS(EX)	Σχ ²	* Nσ _x /ΣX	**° _v /° _•	r	* •	
	2376	5.112	8.961	12146.755	252795. 733	1.753	1.64	.203	1.413	
ľ	4	ΣY/N	σγ	SUM OF N COMPONENTS(ΣΥ)	ΣΥ ²	* Nσ _v /ΣΥ	** V,/v	Σγ	₹ .	
	16	.428	6.798	1015.880	110184.853	15.899	.48	25539	10.7	
-			•	•			•	•	·	

σ Standard devotion of east components

σ Standard deviation of north components

 $[\]sigma_{\mathbf{v}}$ Standard vector deviation of wind velocity

r Correlation coefficient of north and eggt components

V Average wind speed

V Scalar wnd speed

Ratio of standard deviations $= \sigma_{\alpha}/\sigma_{b}$

 $[\]sigma_a$ Standard deviation of wind components along the major axis of the distribution

σ_b Standard deviation of wind components perpendicular to the major αxis of the distribution

Ψ Angle of rotation of the major αxis of tha wind distribution counter-clockwise from E-W direction

[₱] Resultantwind direction

V, Resultant windspeed

o Standard deviation of windspeeds

^{*} Wherever ratio ≥1000.0000, printed 999.9999

^{**} Wherever ratio ≥100.00, printed 99.99